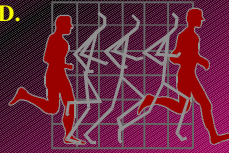


Moment Power Analysis

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Work of a Force

Work of a force is product of force (F) and linear displacement (s) of a body.

$$\begin{aligned}\text{Work} &= F s && \text{(when F is parallel to s)} \\ &= F s \cos \phi && \text{(when F is not parallel to s} \\ &&& \text{and is } \phi \text{ angle between F and s)} \\ \text{or } &= \underline{F} \cdot \underline{s} = F_x s_x + F_y s_y && \text{(dot or scalar product)} \\ &= P t && \text{(average power of force times} \\ &&& \text{duration of force application)}\end{aligned}$$

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2

Work of a Moment of Force

Work of a moment of force is product of moment of force (M) and angular displacement (θ).

$$\begin{aligned}\text{Work} &= M \theta \\ &= r F (\sin \phi) \theta && (\phi \text{ is angle between } r \text{ and } F) \\ &= P t && \text{(mean moment power times} \\ &&& \text{duration)} \\ &= \Sigma (M \omega \Delta t) && \text{(time integral of moment} \\ &&& \text{power)}\end{aligned}$$

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3

Average Power

Power is the rate of doing work.
measured in watts (W), 1 watt = 1 joule per second (J/s)

$$\begin{aligned}\text{Power} &= \text{work} / \text{time} && \text{(work rate)} \\ &= (E_f - E_i) / \text{time} && \text{(change in energy over} \\ &&& \text{time)} \\ &= (F s) / t = F v && \text{(force times velocity)} \\ &= (M \theta) / t = M \omega && \text{(moment of force times} \\ &&& \text{angular velocity)}\end{aligned}$$

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4

Instantaneous Power of a Force or Moment of Force

$\text{Power} = \mathbf{F} \cdot \mathbf{v}$ (when \mathbf{F} is parallel to \mathbf{v})
 $= F v \cos \phi$ (when \mathbf{F} is not parallel to \mathbf{v})
 and ϕ is angle between \mathbf{F} and \mathbf{v}
 $= \underline{\mathbf{F}} \cdot \underline{\mathbf{v}} = F_x v_x + F_y v_y$ (dot or scalar product)
 $= M \omega$ (moment times angular velocity)

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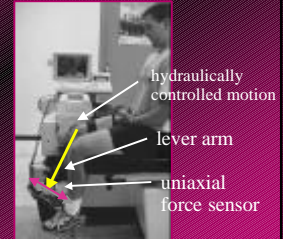
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5

Isokinetic Dynamometers

KinCom 500H

- controls speed of motion therefore lever has constant angular velocity (ω)
- measures force against a lever arm
- moment = force times lever arm
- instantaneous power = moment times angular velocity



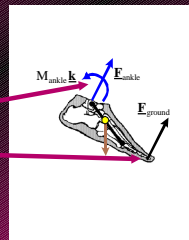
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6

Inverse Dynamics Review

- divide body into kinematic chains
- divide chains into segments
- from free-body diagrams combine forces at each joint into a single "net force and moment of force"
- measure external forces and their points of application
- compute net forces and moments starting at distal segment then proceeding up the chain



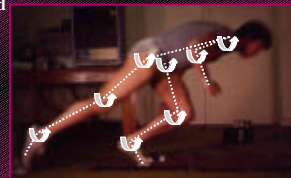
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7

External Work

- Inverse Dynamics Method
 - compute net moments of force at each joint
- Sum over all joint moments and over duration of movement
- External Work = $\Sigma (\Sigma M_j \omega_j \Delta t)$



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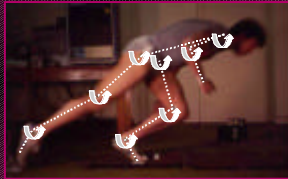
8

Total Mechanical Work

- take absolute values of moment powers
- sum over all joint moments and over duration of movement

• Total Mechanical Work = $\Sigma (\Sigma |M_j \omega_j| \Delta t)$

• Internal work = Total Mechanical Work – External work



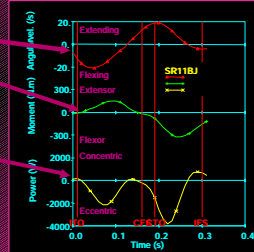
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9

Joint Power Analysis

- compute the angular velocity of the joint
- compute the net moment of force at the joint
- multiply angular velocity and moment of force to obtain the “moment power”
- this is the power produced by the net moment of force acting across the joint
- it is mainly caused by muscle forces



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10

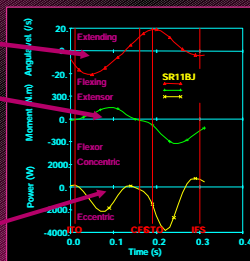
Joint Power Analysis

- angular velocity determines whether joint is flexing or extending

- net moment of force indicates which “muscle group” or “single equivalent muscle” is acting

- moment power tells what the moment of force is doing

- positive power shows “concentric work” while negative power shows “eccentric work”



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11

Limitations

- can only be used on “free-ended” extremities or extremities where external forces can be measured (by force platforms or force transducers)
- assumes elastic storage and release of energy is due to muscle eccentric and concentric work, respectively
- cannot be used with closed kinematic chains (slap shot, golf swing, batting, etc.)
- ignores coactivation of muscles
- assumes no multijoint transfers of energy



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12