

## APA 4311

### Sample Midterm Examination

1. (a) Compute the **radius of gyration** of the swing phase thigh at frame 12 about its centre of gravity.  
 (b) Compute same thigh's **moment of inertia** about its centre of gravity for the same frame.

Total body mass:	70.0 kg		
Camera frame rate:	60.0 frames/second		
	P	R	K
thigh	0.100	0.400	0.600
leg	0.050	0.450	0.500
foot*	0.020	0.500	0.650

P = segment mass as fraction of total body mass  
 R = distance to centre of gravity from proximal end as proportion of segment length  
 K = radius of gyration about centre of gravity as proportion of segment length  
 \* foot's endpoints as ankle and ball

2. Using the anthropometric information and marker coordinates, compute the **segmental and total centres of gravity** of the right (swing phase) limb at frame number 13.
3. Using the tables provided, compute the **linear velocity** of the toes marker of the (swing phase) limb at frame number 13.
4. Using the following tables, compute the **angular acceleration** of the leg of the (stance phase) limb at frame number 13.

	Marker:	Hip	Knee	Ankle	Heel	Ball	Toes	Thigh angle	Leg angle	Foot angle	
Right Limb (swing)	11 X	110.8	107.5	76.7	68.1	78.2	88.9	84.8	42.9	133.7	
	Y	104.3	68.3	34.8	32.4	21.7	18.6				
	12 X	113.6	111.6	79.4	70.6	79.3	89.3	86.7	39.0	125.5	
	Y	104.1	68.0	36.7	35.6	23.4	18.7				
	13 X	116.3	116.0	82.5	73.7	81.0	90.0	89.5	35.0	118.2	
	Y	104.0	67.9	40.7	41.9	27.5	19.4				
Left Limb (stance)	14 X	119.0	120.5	86.0	77.3	83.3	91.6	92.4	31.5	112.6	
	Y	103.9	67.9	40.7	41.9	27.5	19.4				
	15 X	121.6	125.0	89.8	81.2	86.4	94.0	95.5	28.6	109.1	
	Y	103.9	68.1	42.6	44.5	29.5	20.1				
	-----										
	Right Limb (swing)	11 X	114.9	129.4	134.8	129.6	145.2	157.5	113.4	94.5	178.6
		Y	107.5	74.2	27.0	19.5	19.2	21.0			
		12 X	117.2	131.3	134.9	129.5	145.2	157.5	112.9	92.1	178.2
		Y	108.1	74.1	27.0	19.5	19.0	20.7			
		13 X	119.3	133.1	135.0	129.5	145.1	157.5	112.0	90.1	178.1
		Y	108.6	74.6	27.1	19.5	19.0	20.5			
	Left Limb (stance)	14 X	121.5	134.6	135.1	129.5	145.1	157.6	111.0	88.3	178.1
Y		109.0	74.7	27.1	19.5	19.0	20.5				
15 X		134.7	136.0	135.2	129.5	145.1	157.7	109.7	86.7	178.3	
Y		109.4	74.7	65.9	27.2	19.1	20.5				

## Solutions

1.  $\text{length}_{\text{thigh}} = [(113.6-111.6)^2 + (104.1-68.0)^2]^{0.5} = 36.16 \text{ cm}$

(a)  $k_{\text{cg}} = \text{length}_{\text{thigh}} \times K_{\text{cg}} = 21.7 \text{ cm} = 0.217 \text{ m}$

(b)  $I_{\text{cg}} = m_{\text{thigh}} (k_{\text{cg}})^2 = 0.330 \text{ kg.m}^2$

2.  $x_{\text{thigh}} = x_{\text{prox}} + R_{\text{prox.}} \times (x_{\text{dist}} - x_{\text{prox}}) = 116.2 \text{ cm}$

$y_{\text{thigh}} = y_{\text{prox}} + R_{\text{prox.}} \times (y_{\text{dist}} - y_{\text{prox}}) = 89.6 \text{ cm}$

$x_{\text{leg}} = 100.9 \text{ cm}$

$y_{\text{leg}} = 55.7 \text{ cm}$

$x_{\text{foot}} = 81.8 \text{ cm}$

$y_{\text{foot}} = 34.1 \text{ cm}$

$P_{\text{limb}} = P_{\text{thigh}} + P_{\text{leg}} + P_{\text{foot}} = 0.02 + 0.05 + 0.10 = 0.17$

$x_{\text{limb}} = (1.0/P_{\text{limb}}) \times [ (x_{\text{thigh}} \times P_{\text{thigh}}) + (x_{\text{leg}} \times P_{\text{leg}}) + (x_{\text{foot}} \times P_{\text{foot}}) ]$

$y_{\text{limb}} = (1.0/P_{\text{limb}}) \times [ (y_{\text{thigh}} \times P_{\text{thigh}}) + (y_{\text{leg}} \times P_{\text{leg}}) + (y_{\text{foot}} \times P_{\text{foot}}) ]$

$x_{\text{limb}} = (1.0/0.17) \times [ (116.2 \times 0.10) + (100.9 \times 0.05) + (81.8 \times 0.02) ] = 107.6 \text{ cm}$

$y_{\text{limb}} = (1.0/0.17) \times [ (89.6 \times 0.10) + (55.7 \times 0.05) + (34.1 \times 0.02) ] = 73.1 \text{ cm}$

3.  $v_x = (x_{14} - x_{12}) / 2t$

$v_y = (y_{14} - y_{12}) / 2t$

$v_x = (91.6 - 89.3) / (2/60) = 69.0 \text{ cm/s}$

$v_y = (19.4 - 18.7) / (2/60) = 21.0 \text{ cm/s}$

$\underline{v} = (0.690, 0.210) \text{ m/s} \quad \text{or} \quad 0.721 \text{ m/s at } 16.93 \text{ deg}$

4.  $\alpha = [\theta_{11} - (2 \times \theta_{13}) + \theta_{15}] / 4t^2$

$\alpha = [94.5 - (2 \times 90.1) + 86.7] / 4 \times (1/60)^2 = 900 \text{ deg/s}^2 \quad \text{or} \quad 15.71 \text{ rad/s}^2$